

Ecuatii logaritmice – 1 –

$\log_a x = b \Leftrightarrow x = a^b \quad , x > 0, a > 0, a \neq 1, b \in \mathbb{R}$		
Logaritmi – proprietăți		
$\log_a 1 = 0$	$\log_a a = 1$	$\log_a a^n = n$
$\log_a x^n = n \log_a x$	$\log_a \sqrt[n]{x} = \frac{1}{n} \log_a x$	$\log_{a^n} x = \frac{1}{n} \log_a x$
$\log_a x + \log_a y = \log_a xy$	$\log_a x - \log_a y = \log_a \frac{x}{y}$	$\log_a x = \frac{1}{\log_x a} = \frac{\lg x}{\lg a} = \frac{\ln x}{\ln a}$
Rezolvați ecuațiile:		
1.	$\log_2 x = 1$	
2.	$\log_2 x + \log_2(x + 1) = 1$	
3.	$\log_2 x - \log_2(x - 1) = 1$	
4.	$\log_2 x + \log_4 x + \log_8 x = \frac{11}{6}$	
5.	$\log_2^2 x + \log_2 x = 2$	
6.	$\log_x 5 + \log_x 45 = 2$	
7.	$\lg x = -\lg 3$	
8.	$\lg x = -1$	
9.	$\log_2 x = \log_2(x^2 + x - 2)$	
10.	$\log_x 4 = \log_x(x^2 + x - 2)$	
11.	$\log_2 x + \log_x 2 = 2$	
12.	$\log_2 x + \log_3 x = 0$	
13.	$\log_5^2 x - 4\log_5 x + 3 = 0$	
14.	$\ln x = 1$	
15.	$2 \ln x + 1 = 0$	
16.	$\log_2 x(x + 1) = 1$	
17.	$-\log_3^2 x + 11 \log_3 x + 12 = 0$	
18.	$\frac{2 \lg x}{\lg(5x - 4)} = 1$	
19.	$x^{\lg x + 1} = 100$	
20.	$x^{\log_2 x} = 2$	

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|---------------------------|--|-------------------------------------|--|---|
| 1. $x = 2 > 0$            | 2. $x = 1 > 0$                                   | 3. $x = 2 > 1$                      | 4. $x = 2 > 0$                                 | 5. $x \in \left\{ \frac{1}{4}, 2 \right\}$  |
| 6. $x = 15 > 0, x \neq 1$ | 7. $x = \frac{1}{3} > 0$                         | 8. $x = \frac{1}{10} > 0$           | 9. $x = \sqrt{2} > 1$                          | 10. $x = 2 > 1$                             |
| 11. $x = 2 > 0, x \neq 1$ | 12. $x = 1 > 0$                                  | 13. $x \in \{5, 125\}$              | 14. $x = e > 0$                                | 15. $x = \frac{1}{\sqrt{e}} > 0$            |
| 16. $x \in \{-2, 1\}$     | 17. $x \in \left\{ \frac{1}{3}, 3^{12} \right\}$ | 18. $x = 4 > \frac{4}{5}, x \neq 1$ | 19. $x \in \left\{ 10, \frac{1}{100} \right\}$ | 20. $x \in \left\{ \frac{1}{2}, 2 \right\}$ |